Effect of self-generated magnetic fields on fast-electron beam divergence in solid targets

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Abstract. The collimating effect of self-generated magnetic fields on fast-electron transport in solid aluminium targets irradiated by ultra-intense, picosecond laser pulses is investigated in this study. As the target thickness is varied in the range of 25 $\mu$m to 1.4 mm, the maximum energies of protons accelerated from the rear surface are measured to infer changes in the fast-electron density and therefore the divergence of the fast-electron beam transported through the target. Purely ballistic spreading of the fast-electrons would result in a much faster decrease in the maximum proton energy with increasing target thickness than that measured. This implies that some degree of ‘global’ magnetic pinching of the fast-electrons occurs, particularly for thick (>400 $\mu$m) targets. Numerical simulations of electron transport are in good

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agreement with the experimental data and show that the pinching effect of the magnetic field in thin targets is significantly reduced due to disruption of the field growth by refluxing fast-electrons.

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1. Introduction

When a high-power laser pulse with irradiance $> 10^{18}$ W cm$^{-2}$ $\mu$m$^{-2}$ interacts with a solid target, a significant fraction of the laser energy is transferred to the generation of relativistic (fast) electrons. The physics of the transport of the fast-electron beam through the target continues to attract intense interest due to the potential to use electrons to transfer energy from the laser pulse to ignite the compressed fuel in the fast ignition (FI) approach to inertial confinement fusion [1, 2]. The fast-electrons are also responsible for the generation of large space charge fields, which produce and accelerate ions [3].

The divergence (or collimation) of the beam of fast-electrons propagating inside the target is of particular interest as this defines a number of parameters for FI, including the maximum electron source size (hence the laser spot size) and the distance between the electron source and the fuel assembly [4]. Accurate knowledge and control of the fast-electron beam divergence is crucial for a successful demonstration of the electron-based FI scheme and for enhancement of laser-driven ion sources.

When a current of fast-electrons propagates into a solid density plasma, a magnetic field $B$ is generated according to $\partial B / \partial t = - \nabla \times E = - \nabla \times (\eta \cdot j_e)$, where $E$ is the electric field, $j_e$ is the fast-electron current density and $\eta$ is the cold plasma resistivity [5]. This field is azimuthal around the fast-electron beam and gives rise to a ‘global’ pinching effect, which acts to collimate the beam, as described theoretically by Bell and Kingham [6]. Previously, self-generated magnetic fields have been inferred in the work of Tatarakis et al [7] in which plasma jets at the rear side of target foils were observed and recently by Storm et al [8] to explain differences between initial (simulated) and final (measured) fast-electron beam divergence in a solid target (at intensity $\sim 10^{19}$ W cm$^{-2}$). However, there is limited experimental evidence to date on the effectiveness of the field in collimating electrons (in homogeneous solid targets) and on the factors influencing the degree of collimation. In contrast, experimental measurements of Kα emission at the rear surface of metallic targets, typically up to a thickness of $\sim 100$ $\mu$m, suggest that the fast-electron beam has a significant and constant divergence angle, which increases with laser intensity from (half-angle) $\sim 12^\circ$ at $3 \times 10^{18}$ W cm$^{-2}$ to $27^\circ$ at $5 \times 10^{20}$ W cm$^{-2}$ [9].

In this paper, we report on a radically different experimental approach for measuring the effect of magnetic collimation on fast-electron beam transport. This is based on measurements
of multi-MeV proton emission from the rear surface of the target. It is found that the maximum proton energy decreases approximately linearly with the thickness of aluminium targets in the range of 25 µm to 1.4 mm. Purely ballistic spreading of the fast-electrons would result in a much faster fall in the maximum proton energy, and this implies that some magnetic pinching of the fast-electrons occurs. The measurements are found to be in good agreement with numerical calculations performed using a 2D hybrid-Vlasov–Fokker–Planck code called LEDA [5], which also show that electron refluxing [10] can disrupt the growth of the collimating B-field in thin targets.

2. Experimental results

The experiment was performed at the Rutherford Appleton Laboratory using the Vulcan laser, delivering pulses with energy (on the target), $E_L$, up to 280 J, duration, $\tau_L$, equal to 0.7 ps (full-width at half-maximum (FWHM)) and wavelength equal to 1.053 µm. The $p$-polarized pulses were focused with an f/3 off-axis parabolic mirror onto target at an incident angle equal to 13° with respect to the target normal axis, and to a calculated peak intensity of $6 \times 10^{20}$ W cm$^{-2}$. The laser pulse parameters were fixed throughout the experiment. The targets were 3 mm × 7 mm aluminium foils, with thickness, $L$, varied in the range of 25 µm to 1.4 mm. Passive stacks of 5 cm × 5 cm dosimetry film (RCF: Gafchomic© film, HD-810 and MD-V2-55) were positioned 6 cm from the rear of the target (centred on the normal axis to the target) to measure the spatial intensity distribution of the beam of accelerated protons at energies given by the Bragg peak deposition in each piece of film. A 3-mm-wide slot machined in the RCF facilitated a line-of-sight for a Thomson parabola ion spectrometer positioned behind the stack along the target normal axis. Measurements of efficient acceleration of carbon and oxygen ions, sourced from contaminants on the rear surface of the targets, confirm that for the laser and target parameters of this experiment the rear-surface target normal sheath acceleration (TNSA) mechanism [3] dominates.

The most salient result of our investigation is the measured decrease in the maximum proton energy, $E_{\text{max}}$, with increasing $L$, shown in figure 1 (for which good agreement is found between the RCF and Thomson parabola spectrometer measurements). This measurement differs sharply from what is expected on the basis of simple ballistic transport and what has been reported previously for lower laser pulse energies and intensities [11, 12]. Expected $E_{\text{max}}$ as a function of $L$ calculated using a simple model based on ballistic transport is also plotted in figure 1. This model consists of the 1D isothermal plasma expansion formulae derived by Mora [13] (which had been successfully applied previously for similar laser and target parameters [11, 12, 14]), and a variation in the electron density determined by ballistic electron transport through the target at a given constant half-angle of divergence, $\theta_{1/2}$. For the laser pulse parameters used, $\theta_{1/2} \sim 27^\circ$ is expected from the work of Green et al [9]. Calculations for $\theta_{1/2}$ equal to 10° and 16° (as inferred in [8]) are also shown for comparison.

For the purpose of the model calculations, it is assumed that 25% of the laser pulse energy is converted into fast-electrons ($\eta_L \rightarrow e = 0.25$), with mean electron energy $k_B T_e = 7.4$ MeV, as given by ponderomotive scaling [15]. This is assumed to remain constant with increasing $L$, which is justified on the basis of electron transport simulation results discussed later. The number of hot electrons generated is determined to be $N_e = \eta_L \rightarrow e E_L / k_B T_e = 6 \times 10^{13}$. These are assumed to propagate ballistically through the target and form a uniform layer at the rear surface, with density $n_e$ determined by the sheath area. The proton acceleration time $\tau_{\text{acc}}$ is
Figure 1. Maximum proton energy as a function of target thickness. Blue symbols are measurements made using RCF and a Thomson parabola spectrometer (TP-Spec). The error bars include the variation over multiple shots and the energy resolution. The solid lines correspond to calculations using a plasma expansion model assuming ballistic electron transport at given fixed divergence angles. The dashed lines include a correction due to scattering within the target. The red symbols are the result of plasma expansion calculations using electron densities determined from electron transport simulations using the LEDA code.

1.3τ_L, as used previously by Fuchs et al [12]. Variation of the parameters η_L→e and τ_acc changes the predicted maximum proton energies, but does not significantly change the overall shape of the predicted E_max as a function of the L curve and cannot reproduce the measurements.

Adjustments to the plasma expansion model calculations to account for electron scattering from target atoms are also shown in figure 1 (dashed lines). These are estimated using the Monte Carlo code GEANT4 [16]. A group of 8 MeV electrons are propagated through a 2 mm aluminium target and the lateral extent of the scattered electrons is calculated as a function of distance. This has the effect of reducing n_e and therefore E_max.

We have also considered the interplay between the fast-electron angular distribution as a function of energy and electron stopping within the target. If the electron beam divergence decreases with increasing energy, the increased stopping of low-energy electrons within the target may reduce the overall transverse extent of the fast-electron distribution as the target thickness is increased. To investigate whether this effect could account for the measured distribution, we calculate the expected E_max as a function of L assuming different distributions of electron divergence angle with energy and incorporating electron stopping. Three different injection functions are modelled as shown in figure 2(a). ‘Injection 1’ corresponds to a constant divergent angle, resulting in a uniform electron density at the target rear as shown in figure 2(b). This is the distribution used in the calculations shown in figure 1. The divergence angle decreases linearly with energy for ‘Injection 2’, which results in a parabolic-like sheath profile, and ‘Injection 3’ corresponds to an exponential decrease in divergence angle with energy and results in an approximately trapezoidal sheath profile, as shown in figure 2(b). The effects of fast-electron stopping within the target are included in the calculations. An electron with a kinetic energy of 1 MeV has a stopping distance of about 2 mm [17] and hence the bulk of the fast-electrons pass through the target with little energy loss. Furthermore, because the target is a metal, the effects of resistive inhibition [18] are minimized. The results of applying the Mora
Figure 2. (a) Example distributions of injected fast-electron beam divergence with energy. (b) The corresponding electron density distribution at the rear surface of a 300 µm-thick target. (c) The resulting maximum proton energies as a function of target thickness as calculated using the Mora plasma expansion formulae. The calculations include the effects of electron stopping in the target.

plasma expansion formula for the densities determined with the three different injected electron distributions (assuming $k_B T_e = 7.4$ MeV and $\tau_{acc} = 1.3 \tau_L$, as discussed above) are shown in figure 2(c). The electron divergence distribution clearly affects the maximum proton energy, but does not account for the nearly linear decrease in $E_{max}$ with $L$ measured.

As clearly shown, the measured dependence of $E_{max}$ on $L$ cannot be explained by ballistic transport of fast-electrons through the target at a constant angle of divergence. In order to reproduce the results the electron beam divergence must decrease with increasing $L$. The implication is that self-generated fields in the target must be reducing the transverse spreading of the beam (particularly in thicker targets). Magnetic collimation is the obvious candidate for this effect.

3. Model of sheath evolution and proton acceleration

To quantify the change in the transverse size of the initial electron sheath (before expansion) with $L$, the sheath and ion front evolution in space and time are modelled and the resulting ion beam parameters compared to the measurements, using an approach similar to that reported by Carroll et al [19]. The model of the sheath evolution involves three considerations: (i) the initial sheath shape; (ii) the sheath transverse expansion velocity as a function of time; and (iii) the temporal evolution of the magnitude of the sheath electric field. The initial sheath field shape is assumed to be parabolic based on the conclusions of Brambrink et al [20]. We also considered Gaussian and hyperbolic sheath profiles, but find that these do not reproduce the measured proton beam divergence as a function of energy. The initial transverse sheath expansion velocity is set equal to $c$, as reported in previous work for very similar laser parameters [21, 22], and decreases exponentially with time, with $1/e = 1.6$ ps, consistent with optical probe reflectometry measurements of Antici et al [23]. The field strength increases with the rising edge of the laser pulse with a Gaussian profile to a maximum value set by the measured $E_{max}$ and follows an exponential decrease thereafter (with $1/e = 1.6$ ps), as also inferred from previous work [21, 24]. The evolution of the field in space (transverse expansion of the sheath
Figure 3. Comparison of (a) proton beam divergence and (b) proton source size as calculated using the sheath expansion model with measurements made by irradiation of a target with linear grooves machined into the rear surface. (c) Initial electron sheath size as a function of target thickness. Blue symbols result from the application of the model to the experiment data. The error bars include the variation over multiple shots and the energy resolution of each piece of RCF film. The solid lines correspond to ballistic electron transport at given fixed divergence angles. The dashed lines include a correction due to scattering within the target. The red symbols correspond to the lateral extent of the fast-electron beam (at the point in time when the electrons reach the rear surface) in 2D LEDA hybrid simulations.

Field ionization of a uniform layer of hydrogen is invoked to define an ion front [25]. The spatial extent and profile of the expanding ion front, and thus the emitted angle of protons produced along the front, are calculated as a function of time. The resulting maximum angle of divergence as a function of proton energy is compared with the measurements. The initial sheath size at FWHM, $D_e$, is varied until the calculated divergence–energy profile matches the measured profile, as shown in the example in figure 3(a). The process is repeated for each target thickness.
To test the sheath evolution model, the calculated proton source size and divergence as a function of energy are both compared with direct measurements using a 25 µm-thick Au target with lines (grooves with separation equal to 10 µm and depth equal to 1 µm) manufactured into the rear surface [26]. The line structure is mapped onto the measured proton spatial intensity profile and the source size as a function of energy is determined by counting the lines in each RCF layer [26]. As shown in figure 3(b), the calculated proton source size as a function of energy is in excellent agreement with the measurement when $D_e$ is varied to provide a best fit to the measured proton beam divergence as a function of energy—figure 3(a).

Figure 3(c) shows the resulting $D_e$ as a function of $L$. For relatively thin targets ($L < 300 \mu m$) the increase in $D_e$ with increasing $L$ is consistent with an approximately constant divergence angle of $\sim 27^\circ$. A transition is observed at about 300–400 µm, above which the growth in $D_e$ with $L$ is much lower than expected from ballistic transport. This reduction in the effective beam divergence in thick targets is likely to result from the pinching effect of the azimuthal $B$-field resistively self-generated by the fast-electron beam [6].

The growth of the self-generated $B$-field is governed by the electron beam and target material properties [6] and should be independent of target thickness, particularly as the field is strongest close to the electron source (where the current density is highest). The apparent lack of beam pinching for $L < 300 \mu m$ may be related to electron refluxing within the target during the laser pulse duration [10]. Counter-streaming fast-electrons act to locally cancel out the net forward fast-electron current in thin targets, disrupting the growth and therefore the pinching effect of the $B$-field.

4. Electron transport simulations

If a ‘global’ pinching of the fast-electron beam due to self-generated magnetic fields is responsible for the reduction in the transverse extent of the fast-electron population in thick targets, then this should be apparent in numerical simulations. The 2D hybrid-Vlasov–Fokker–Planck code called LEDA was used to carry out a set of fast-electron transport simulations to investigate this.

The code is described in detail elsewhere [5]. The fast-electrons are injected at the left-hand end of the grid, in a pulse with duration equal to 0.7 ps. The fast-electron distribution is a relativistic Maxwellian of the form $(\cos^M\theta) p^2 \exp(-((p^2 + m_e^2 c^2)^{1/2}) / k_B T_e)$, with $k_B T_e = 9$ MeV. We note that this is slightly higher than the temperature of the fast-electron distribution expected in the experiment. However, comparative example simulation runs with $k_B T_e = 7.4$ MeV show that this small temperature difference does not significantly affect the simulation results (nor the conclusions of this work). The injection angle is set at $M = 8 (\sim 24^\circ$ half-angle). The conversion efficiency $\eta_{L\to e} = 0.25$ and the initial background temperature is set to 1 eV. A uniform spatial grid is used for all the simulation runs, with a cell size equal to 1 µm. The number of cells in $y$ is typically 480, and the cell number in $x$ is varied between 80 and 800, to simulate the variation in $L$. All other parameters are fixed.

Figure 4(a) shows a map of the simulated magnetic flux density at 1.4 ps after laser irradiation of a 300 µm Al target. This illustrates the azimuthal profile of the self-generated field, which extends $\sim 100 \mu m$ from the electron source. Figure 4(b) shows the simulation result for an 80 µm Al target for otherwise identical conditions. After 1.4 ps the refluxing electrons, which are reflected in the sheaths formed on both sides of the target, have made multiple passes.
through the thinner target and the resulting $B$-field is considerably fragmented, reducing its effectiveness in collimating electrons.

Two main parameters of interest are extracted from the results of the main simulation runs. The first is the average fast-electron density on-axis ($y = 0$) at the rear surface of the target, which is plotted in figure 4(c) as a function of $L$. A change in the rate of decrease is observed at $L \approx 400 \mu m$. These values of $n_e$ are used with the Mora [13] plasma expansion formulae (with the same assumptions and input parameters discussed above) to calculate $E_{\text{max}}$. The results are found to be in excellent agreement with the experimental results, as shown in figure 1. The second parameter extracted is the lateral extent (full-width) of the beam of fast-electrons as they reach the target rear surface and before any reflection has occurred (the simulation output time at which the distribution is sampled increases with $L$ accordingly). As shown in figure 3(c), although smaller than the initial sheath size extracted from the sheath evolution model fit to the experimental data, a similar overall increase in sheath size with $L$ is observed, including the differences between thinner and thicker targets.

The LEDA results are, in both cases, in good agreement with the experimental results. This is particularly so in the case of the maximum energies (see figure 1). On examining the LEDA simulations it is clear that the magnetic field is constraining the transverse extent of the fast-electron beam and thus maintaining the on-axis fast-electron density.

As mentioned previously, one of the assumptions implicit in this work is that the fast-electron temperature at the target rear surface does not change significantly with $L$. The results of the LEDA simulation runs confirm that this assumption is valid, as shown in figure 4(d) by the two example electron spectra sampled on-axis at the target rear surface for $L=400$ and 800 $\mu$m. The fast-electron density is reduced for the thicker target, but a significant change in $k_B T_e$ is not observed.

5. Summary

In summary, we report on an experimental investigation of the effect of magnetic collimation on fast-electron transport using measurements of multi-MeV proton emission. A key advantage of this novel diagnostic approach is that it is directly sensitive to the density of fast-electrons at the target rear surface. Using this approach we obtain evidence that some magnetic pinching of the fast-electron beam occurs in thick metallic targets. The results are found to be in good agreement with fast-electron transport simulations, which further show that fast-electron refluxing within thin targets disrupts the field growth.

A detailed assessment of the implications of these results for FI is beyond the scope of this paper. However, we briefly consider two points. Firstly, FI is likely to require laser pulses with duration between 5 and 10 ps and intensity $\sim 3 \times 10^{19}$ W cm$^{-2}$ to produce electrons with $k_B T_e \approx 1.2$ MeV [4]. According to the Bell–Kingham criteria [6] the degree of self-collimation increases both for longer pulse duration and lower electron temperature. Secondly, the FI fuel target has a low effective $Z$, which may reduce the magnitude of the self-generated $B$-field [6]. A detailed investigation of the scaling of the self-generated field and resulting electron beam collimation to FI conditions is the subject of future work.

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