Developed turbulence and non-linear amplification of magnetic fields in laboratory and astrophysical plasmas

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The visible matter in the Universe is turbulent and magnetized: turbulence in galaxy clusters is produced by mergers and by jets of the central galaxies and believed responsible for the amplification of magnetic fields. We report on experiments looking at the collision of two laser-produced plasma clouds, mimicking in the laboratory a cluster merger event. By measuring the spectrum of the density fluctuations, we infer developed, Kolmogorov-like turbulence. From spectral line broadening, we estimate a level of turbulence consistent with turbulent heating balancing radiative cooling, as it likely does in galaxy clusters. We show that the magnetic field is amplified by turbulent motions, reaching a nonlinear regime that is a precursor to turbulent dynamo. Thus, our experiment provides a promising platform for understanding the structure of turbulence and the amplification of magnetic fields in the Universe.

Keywords: Turbulence, Galaxy clusters, Magnetic field amplification
Significance statement

Magnetic fields exist throughout the Universe. Their energy density is comparable to the energy density of the fluid motions of the plasma in which they are embedded, making magnetic fields essential players in the dynamics of the luminous matter in the Universe. The origin and the amplification of these magnetic fields to their observed strengths are far from being understood. The standard model for the origin of these galactic and intergalactic magnetic fields is through the amplification of seed fields via turbulent processes to the level consistent with current observations. For this process to be effective the amplification needs to reach a strongly non-linear phase. Experimental evidence of the initial non-linear amplification of magnetic fields is presented in this paper.
In the early universe, matter was nearly homogenously distributed; today, as a result of gravitational instabilities, it forms a web-like structure consisting of filaments and galaxy clusters [1]. The continued mergers of galaxies, filaments, and galaxy clusters inject turbulence into the intergalactic medium via shocks [2, 3]. At the same time, the existence of diffuse synchrotron emission at radio wavelengths and Faraday rotation measurements indicate the presence of magnetic fields in galaxy clusters with strengths up to tens of µG [4, 5]. The standard model for the origin of these intergalactic magnetic fields is amplification of seed fields via the turbulent dynamo mechanism to the present-day observed values [6, 7, 8, 9, 10], but other possibilities involving plasma kinetic instabilities [11, 12, 13, 14], return currents [15, 16] or primordial mechanisms [17, 18] have also been invoked.

We have carried out experiments involving the collision of two plasma jets – reminiscent of cluster merger events – to produce a laboratory-scale replica of a turbulent intracluster plasma, although obviously our plasma is not confined in a dark matter potential well, as it is in clusters. In the intracluster medium, large-scale turbulent motions are influenced by density stratification and gravity. However, at smaller spatial scales the time periods for buoyancy-driven motions are much longer than those of the turbulent motions, so the fluctuations at these scales are universal, and thus similar to the turbulence we can create in our laboratory experiments. The scale invariance of hydrodynamic equations [19, 20] implies, if we assume that a distance of 1 cm in the laboratory corresponds to 100 kpc in the astrophysical case, that 1 µs becomes 0.5 Gyr and a density of $4 \times 10^{17} \text{ cm}^{-3}$ is equivalent to 0.01 cm$^{-3}$ in the galaxy cluster.

Our experiments were conducted using the Vulcan laser of the Central Laser Facility at the Rutherford Appleton Laboratory. We have focussed multiple laser beams (with ~240 J total energy and ~1 ns pulse duration) onto a carbon foil to launch a plasma jet into an ambient argon gas-filled chamber (at a pressure of 1 mbar). A full description of the experimental setup is given in Fig. 1. Ablation of target material by the laser drives a shock into the carbon
foil, which then produces a collimated jet from the back surface of the target (i.e., the side opposite to that illuminated by the laser). The target material ablated by the laser is slowed by the ambient medium, creating a wrap-around shock, visible in Fig. 1. Schlieren measurements were taken to characterize the outflows at various times. The fastest moving material occurs on axis (see Fig. 2) with $v_0 \sim 25$ km/s ($v_0/c_s \sim 4$, where $c_s$ is the sound speed) at 3 cm from the target, while material on the edges of the jet moves more slowly as a result of Kelvin-Helmholtz shearing instabilities. Experiments were also performed using two sets of laser beams, each set illuminating a carbon foil, producing two jets that collide. The collision drives strong turbulence in a region that grows from a size $L \sim 1$ cm at $t = 0.8$ µs to $\sim$ 2 cm at $t > 1.5$ µs, at which time the turbulence reaches a more relaxed state.

The turbulent velocity fluctuations on the system scale $L$ can be estimated from Fig. 2b. At the collision point, the observed argon emission lines are broadened by $\sim 0.2$ nm. Half of this broadening is attributed to the increased density, and to a lesser extent to the higher temperatures (thermal broadening is small due to the large ion mass) – see supplementary material. The broadening due to turbulent motions is then $\sim 0.1$ nm, corresponding to a turbulent velocity $v_{turb} \approx 27 \pm 5$ km/s. Thus, $v_{turb} \sim v_0$, suggesting that the collision effectively randomizes the directed velocities of the two jets. Taking the measured values of jet velocity, density, and temperature in the collision region, and assuming an ionization state $Z \sim 2.5$ for argon, we estimate the inter-jet electron-ion ($\lambda_{ei} \approx 0.04$ cm) and ion-ion ($\lambda_{ii} \approx 0.005$ cm) mean free paths to be significantly smaller than the size of the jets. This confirms that the two jets strongly interact via Coulomb collisions and the contact surface between the two jets becomes quickly unstable. The Reynolds number calculated with respect to the scale $L$ is thus $Re = v_{turb}L/\nu \sim 1.0 \times 10^6$ ($\nu \approx 2.8$ cm$^2$/s is the kinematic viscosity of the plasma).

For our plasma conditions the radiative cooling rate per ion is $Q_{cool} \sim m_{ion}\kappa_P\sigma_{SB}T^4 \sim 0.5$ eV/ns, where $m_{ion}$ is the argon mass, $\kappa_P \sim 8 \times 10^4$ cm$^2$/g is the Planck opacity (see sup-
plementary information), and $\sigma_{SB}$ is the Stefan-Boltzmann constant. This implies that during one jet crossing time, $\sim L/v_0 \approx 400$ ns, the plasma should have cooled to near 1 eV, as in the case of a single jet expansion (detailed calculations are provided in the supplementary information). Fig. 2 instead shows that in the collision region the temperature remains $\gtrsim 2$ eV over a few $L/v_0$, suggesting that much of the cooling must be offset by heating. Turbulent motions are eventually dissipated into heat. This heating rate per ion can be approximated to be $Q_{turb} \sim m_{ion}v_{turb}^3/L \sim 0.6$ eV/ns. Thus $Q_{turb} \sim Q_{cool}$, consistent with turbulence playing an important role in achieving a stable temperature profile, with near balance between turbulent heating and radiative cooling.

We performed simulations of the experiments using the FLASH code [21, 22] (see supplementary material). The results of the FLASH simulations are consistent with the measured properties of the jet, including its morphology and the physical conditions in the interaction region (Figs. 1 and 2). The simulations indicate enhanced vorticity as the two jets collide, and reproduce the increase in the electron density and the moderate rise in the temperature after the collision.

In some respects, our experimental conditions are qualitatively similar to those found in galaxy cluster, where heating driven by turbulent motions in the intracluster plasma reduces radiative losses and decreases the net cooling rate [23]. On the other hand, while in the inertial range energy is transferred from one scale to another at a rate given by $Q_{turb}$, which has the same form both in clusters and laboratory experiments, the actual mechanism for energy dissipation into heat can be different. This is dominated by collisional, isotropic viscosity in the laboratory, whereas in clusters, at a minimum, one must take into account that viscosity is anisotropised due to magnetic fields and furthermore kinetic processes may play an important role [8]. Thus the similarity between the laboratory “replica” and the astrophysical reality can only hold at scales larger than the viscous one.
During hierarchical structure formation, clusters form from accretion of filaments, galaxies, galaxy groups, and cluster mergers. In clusters of galaxies, turbulent velocities can be inferred from the density perturbations, which, in turn, are obtained using the measured X-ray radiation intensities [23, 24, 25]. The turbulence in clusters is mainly sub-sonic at small scales (and near sonic at large scales), so density fluctuations (injected at large scales) behave like a passive scalar. Therefore the density and velocity spectra are expected to be the same [26]. The fact that turbulence is moderately supersonic in our experiment while sub-sonic in clusters, is likely to lead to only a modest change in the power spectra (and at small enough scales, motions will in any event become sub-sonic). Indeed, spectroscopic observations of supersonic motions in molecular clouds [27] suggest a velocity power spectrum close to the classical Kolmogorov $k^{-5/3}$ law (where $k$ is the wavenumber) that holds for incompressible fluids. Numerical simulations of supersonic turbulence show a spectrum somewhat steeper than Kolmogorov’s, $k^{-1.7}$ to $k^{-2}$, depending on the details of the driving mechanism [28]. These differences are smaller than the uncertainties in our power spectrum measurements.

We have extracted the power spectrum of the electron density fluctuations from our data. The result is shown in Fig. 3a, using the wavelet method discussed in Ref. [25], which was used there for the analysis of X-ray maps of the Coma cluster. The spectrum is consistent with a Kolmogorov-like power law as expected from the theoretical work we discuss above, suggesting that we do indeed see fully developed turbulence. A similar spectrum was obtained in galaxy clusters [24, 25].

While $Re \gg 1$ and turbulent motions are excited over a large range of scales, the magnetic Reynolds number is $Rm = \nabla_{turb}L/\eta \sim 14$ ($\eta = 1.9 \times 10^5$ cm$^2$/s is the resistivity), so the resistive scale lies well above the viscous scale, and close to the system scale, $L$. Since $Rm$ is not very large in the experiment, the full magneto-hydrodynamic (MHD) scaling between the cluster and the laboratory is only marginally valid [20]. At such $Rm$, turbulent dynamo,
believed to be the mechanism whereby strong fields are generated in galaxy clusters [8, 7], does not operate, but the magnetic fields can be amplified via stochastic tangling of an imposed field by turbulent motions [29, 30]. At small Rm (≤ 1), the amplified field grows proportionally to Rm and has the Golitsyn [29] $k^{-11/3}$ power law, which arises in Kolmogorov turbulence when the stochastic tangling of the magnetic field is balanced by Ohmic diffusion. As Rm gets larger the scaling of the amplified field gets closer to $Rm^{1/2}$, and its spectrum becomes shallower [31]. Eventually, there is a transition to the turbulent dynamo regime, expected at $Rm \sim 200$.

In our experiment, magnetic fields are generated before the collision via the Biermann battery mechanism [32, 33], which is sustained by the shearing instability between the jet and the ambient medium. It is this field that is then tangled and amplified by turbulent motions. Fig. 4 shows that the magnetic field is larger by a factor ~2-3 in the case of collision of the two jets compared to the unperturbed single jet. The FLASH simulation reproduces the morphology and time behavior of the magnetic field, including the time at which the field changes sign. We expect the simulation to underpredict the peak magnetic field in the colliding jets case since turbulent amplification is not properly captured in 2D geometry.

Most importantly, the amplified magnetic field detected in the experiment is larger than the Biermann battery produced field. This suggests that amplification has reached the non-linear regime, with the amplified field roughly proportional to $Rm^{1/2}$. This conclusion is further supported by measurement of the magnetic energy spectrum $M(\omega)$, shown in Fig. 3b. Translated into wavenumber spectrum, this spectrum is $M(k) \sim k^{-17/9}$ (see the supplementary material), substantially shallower than the low-Rm Golitsyn spectrum $k^{-11/3}$ [29], which we observe in the case of no jet collision, so both less turbulence and lower Rm [10]. The emergence of progressively shallower magnetic spectra is a sign of nonlinear field amplification, which is a precursor to turbulent dynamo [31].

Despite important differences, the laboratory simulation of an intracluster plasma that we
have created offers a new tool for modelling the amplification of magnetic fields by turbulent astrophysical plasmas.

**References and Notes**


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Author Contributions

Figure Legends

Figure 1: **Colliding jet configuration for the generation of turbulence.** Two carbon foils (100 μm thick, with density 1.13 g/cm³) are separated by 60 mm in a 1 ± 0.2 mbar argon gas-filled chamber. Each target is ablated by three frequency doubled (527 nm wavelength) laser beams with a laser spot diameter of 300 μm. The total laser illumination onto each foil is 240±30 J in a 1 ns pulse length. An induction coil (>200 MHz bandwidth, with four twisted pair coils wound around the axis of a ~1×1 mm² plastic core) is placed at equal distance between the foil targets. Additional details are given in Ref. [10]. (a) Schlieren image (using a 532 nm wavelength probe and 5 ns CCD gate width) of the jet formations at t = 500 ns after the laser shot. (b) The jets collide at t = 800 ns, and (c) turbulence develops by t = 1500 ns. (d) Magnetic field (top) and mass density (bottom) from a FLASH simulation of the two jets at t = 500 ns. (e) Same as (d) but at t = 800 ns. (f) same as (d) but at t = 1500 ns. (g) Schlieren synthetic image obtained by post-processing the FLASH results at t = 500 ns using Spect3D [34]. (h) Same as (g) but at t = 800 ns. (i) same as (g) but at t = 1500 ns. The measured and simulated Schlieren images are similar at t = 500 and 800 ns, but differ at t = 1500 ns. The difference is likely due to a slight angle between the directions the two jets are moving, which allows part of the jets to continue beyond the initial interaction region. This produces a much larger turbulent region in the experiment than in the simulation, where the 2D cylindrical geometry prevents us from accommodating this situation. Since the FLASH simulations are 2D cylindrical, the plane that most closely corresponds to the experimental data is the one that is perpendicular to the page and connects the two target foils. This plane does not contain the induction coil probe.
Figure 2: **Characterization of jet propagation and collision.** (a) Measurement of the jet leading edge vs time from Schlieren data (blue symbols) and FLASH simulations (dashed green line). The FLASH simulation was calibrated to match the position of the leading edge of the jet at 800 ns for the measured value of the total laser energy for that data point. The inset shows the electron density profile obtained by interferometry at $t = 800$ ns compared to FLASH predictions. The density has been averaged over a volume of 5 mm radius from the axis connecting the two target foils. (b) Spatially resolved electron temperature profile of a single jet (blue symbols) and colliding jets (red symbols) at $t = 800$ ns obtained from the measured argon spectral lines (see supplementary information for details). Solid lines (blue: single jet; and, red: colliding jets) correspond to the predicted temperature values from FLASH simulations at $t = 800$ ns, averaged over the same volume as the electron density. Dashed lines are the results from the same FLASH simulations at $t = 1500$ ns. The inset shows an example of the argon spectral line at $t = 800$ ns and 3 cm from the carbon foil target (averaged over 0.1 cm).
Figure 3: **Power spectra of turbulence.** (a) Plot of the density fluctuation power spectrum \( P(k) = |n_k/n_0|^2 \), where \( n_k \) is the discrete Fourier transform of the space-dependent electron density and \( n_0 \) its average value. In Schlieren imaging, the measured signal intensity is proportional to \( \int (\partial n/\partial y + \partial n/\partial z) dx \), where \( n \) is the electron density, \( x, y \) are the image-plane spatial co-ordinates and \( z \) the depth [35]. Therefore, under the assumption that turbulence is statistically homogeneous across the jet interaction region, the discrete Fourier transform of the central region of the jet collision in Fig. 1c directly gives \( n_k \). The power spectrum is arbitrarily normalized so that \( P(k) \approx 1 \) at the largest scale. The solid red curve corresponds to the experimental data, while the black and green symbols correspond to the inferred density spectrum in the Coma cluster obtained from CHANDRA and XMM satellite observations, respectively [25]. (b) Plot of the magnetic energy spectrum \( M(\omega) = |B(\omega)|^2 \), where \( B(\omega) \) is the discrete Fourier transform of the total magnetic field for both the cases with a single jet (red solid line) and with colliding jets (blue solid line). The slope of the spectrum in the case of colliding jets is shallower than in the case of a single jet (where it is consistent with the \( k^{-11/3} \) Golitsyn spectrum, assuming conversion from frequencies to wave numbers according to Taylor hypothesis, \( \omega \sim v_0 k \)). This gradual shallowing of the spectrum with increasing \( Rm \) is a signature of the dynamo precursor regime [31]. The measured frequency spectrum \( \sim \omega^{-7/3} \) can be argued to correspond to wavenumber spectrum \( \sim k^{-1.9} \) in the case of colliding jets, where Taylor hypothesis is inapplicable (see supplementary information).
Figure 4: **Time evolution of the magnetic field.** (a) The magnetic field components measured at 3 cm from the carbon foil in the case of a single jet (see Fig. 1 for the axis co-ordinates). (b) Magnetic field components measured in the case of jet collision. The time resolution of the magnetic field traces is 10 ns. These have been extracted from the recorded induction coil voltages. Details are given in Ref. [10]. The initial ($t < 100$ ns) high frequency noise due to the laser-plasma interaction with the target has been filtered. The dashed lines in both panels correspond to the average azimuthal magnetic field obtained from the FLASH simulations in a volume of radius 1 mm and length 3 mm centered at the midpoint between the two target foils. Due to cylindrical symmetry of the simulation domain, the measured component that is closest to the calculated one is $B_z$. 